

# Hamada's formula

L<sup>A</sup>T<sub>E</sub>X exercise

In the formula below,  $\dim C^*(r, n, q)$  is the rank over  $\mathbf{F}_p$  of a certain matrix.

For  $q = p^h$  with  $p$  prime,

$$\dim C^*(r, n, q) = \frac{q^{n+1} - 1}{q - 1} - \sum_{(s_0, \dots, s_h)} \prod_{j=0}^{h-1} \sum_{i=0}^{L(s_{j+1}, s_j)} (-1)^i \binom{n+1}{i} \binom{n + s_{j+1}p - s_j - ip}{n},$$

where the first sum is over all ordered sets  $(s_0, \dots, s_h)$  of  $h+1$  integers  $s_j$  such that

$$s_h = s_0, \quad 0 \leq s_j \leq n - r, \quad 0 \leq s_{j+1}p - s_j \leq (n+1)(p-1),$$

and

$$L(s_{j+1}, s_j) = \lfloor (s_{j+1}p - s_j)/p \rfloor.$$